## Checsup

## Increasing or decreasing by a percentage

a) The following prices are exclusive of VAT, which has to be added at $17 \frac{1}{2} \%$. What is the overall cost of each? Use a calculator only for the second example.
i) A television monitor listed at $£ 320$
ii) A printer listed at $£ 196.50$
b) A secondary school has 87 unauthorised absences in one term. To achieve at least a $12 \%$ reduction in this figure, what is the school's target for unauthorised absences the following term? Do this both without and with a calculator.
c) One year a primary school has $67 \%$ of pupils achieving level 4 or above in the Key Stage 2 English test. What would be their target for next year in order to increase this figure by 10 percentage points? What would be their target to increase it by $10 \%$ ?

## Answers to check-up 33

a) i) $£ 376$.
ii) $£ 230.89$.
b) 76 .
c) $77 \%, 73.7 \%$.

## Discussion and explanation of check-up 33

Problems about percentage increases and decreases always contain three elements: the starting value, the percentage change and the finishing value. There are, therefore, basically three types of problems: (i) given the starting value and the percentage change, to find the finishing value; (ii) given the starting value and the finishing value, to find the percentage change; (iii) given the percentage change and the finishing value, to find the starting value. This check-up deals with the first of these.
a) To find $17 \frac{1}{2} \%$, we can piece together $10 \%, 5 \%$ and $2 \frac{1}{2} \%$, which is easy to do mentally for $£ 320$. $10 \%$ of $£ 320$ is $£ 32$, so (halving this) $5 \%$ is $£ 16$ and (halving again) $2 \frac{1}{2} \%$ is $£ 8$. So the increase is $£ 32+£ 16+£ 8=£ 56$, giving the finishing price as $£ 376$. The calculation of $17 \frac{1}{2} \%$ of $£ 196.50$ is a bit tricky to do mentally, so we'll use a calculator. Now the obvious approach is to use the calculator to find $17 \frac{1}{2} \%$ of $£ 196.50$ and then use the calculator again to add this on to the $£ 196.50$. But there's a quicker way that I always use. When we have added on the $17 \frac{1}{2} \%$ we will then have $117 \frac{1}{2} \%$ of what we started with. So I can go straight to the finishing price just by calculating $117 \frac{1}{2} \%$ of $£ 196.50$. I can do that on a calculator in just one step, by converting the percentage (117.5\%) to a decimal (1.175), giving $196.50 \times 1.175=230.8875$, which rounds to $£ 230.89$.
b) You can find $12 \%$ of 87 mentally by piecing together $10 \%, 1 \%$ and $1 \%$. That gives us $8.7+0.87+0.87=10.44$. We will have to round this $u p$ to 11 to achieve the target reduction. Subtracting this from 87 gives the target as 76 . Doing this with a calculator, we could say that the target for next term is $88 \%$ $(100 \%-12 \%)$ of the figure for this term. Since $88 \%=0.88$ we can do this just by entering this one calculation: $87 \times 0.88$. This gives 76.56 , so the target is 76 .
c) When the starting and finishing values are themselves percentages, there can be confusion when we talk about percentage changes. To increase the $67 \%$ by 10 percentage points means just to add $10 \%$ to the $67 \%$, giving $77 \%$. The $10 \%$, $67 \%$ and $77 \%$ are all percentages of the whole quantity or set. But if we say that we aim to increase the score of $67 \%$ by $10 \%$ we mean that the $10 \%$ increase is $10 \%$ of the $67 \%$, i.e. $6.7 \%$. This gives a finishing figure of $67 \%+6.7 \%=73.7 \%$.

## Summary of key ideas

- VAT at $17 \frac{1}{2} \%$ can be found mentally by piecing together $10 \%, 5 \%$ and $2 \frac{1}{2} \%$.
- Many percentage increases and decreases can be calculated mentally by such informal methods (e.g. a decrease of $18 \%$ can be worked out as $10 \%+5 \%+1 \%+2 \%)$.

The finishing value after a percentage increase or decrease can be found on a calculator in one step (e.g. to increase by 27\% multiply by 1.27 ; to decrease by $27 \%$ multiply by 0.73 ).

- If the starting and finishing values are themselves percentages, then increasing or decreasing by a number of percentage points is not the same as increasing or decreasing by a percentage (e.g. $80 \%$ decreased by 5 percentage points is $75 \%$, but $80 \%$ decreased by $5 \%$ is $76 \%$ ).


## Further practice

33.1 In the Key Stage 1 writing task, $56 \%$ of a primary school's Year 2 pupils achieve level 2 or above. What would this be next year if the school were to achieve an increase of 5 percentage points? What would it be if this figure were increased by $5 \%$ ? (No calculator required.)
33.2 What would you enter on a calculator to find the result of increasing 6543 by $21 \%$ ? And what would you enter to find the result of decreasing 6543 by $21 \%$ ?
33.3 A computer is listed at $£ 789$, to which must be added VAT at $17 \frac{1}{2} \%$. The firm offers schools a reduction of $12 \%$. Would you prefer the VAT to be added first or the reduction to be applied first? Answer this intuitively and then use a calculator to work it out.

